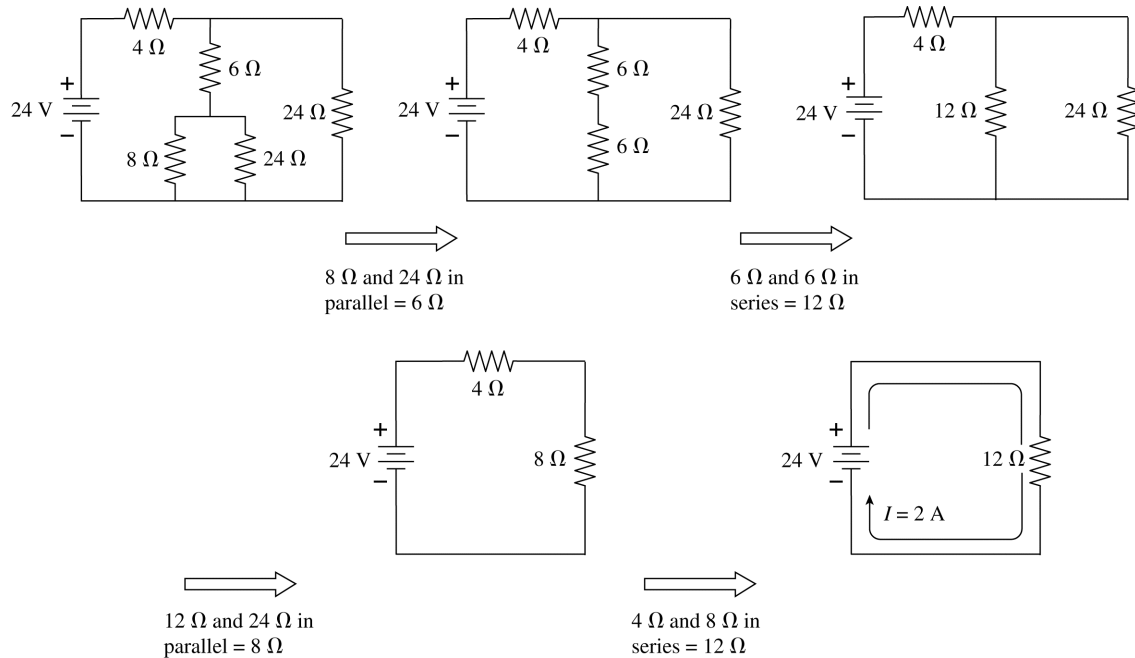


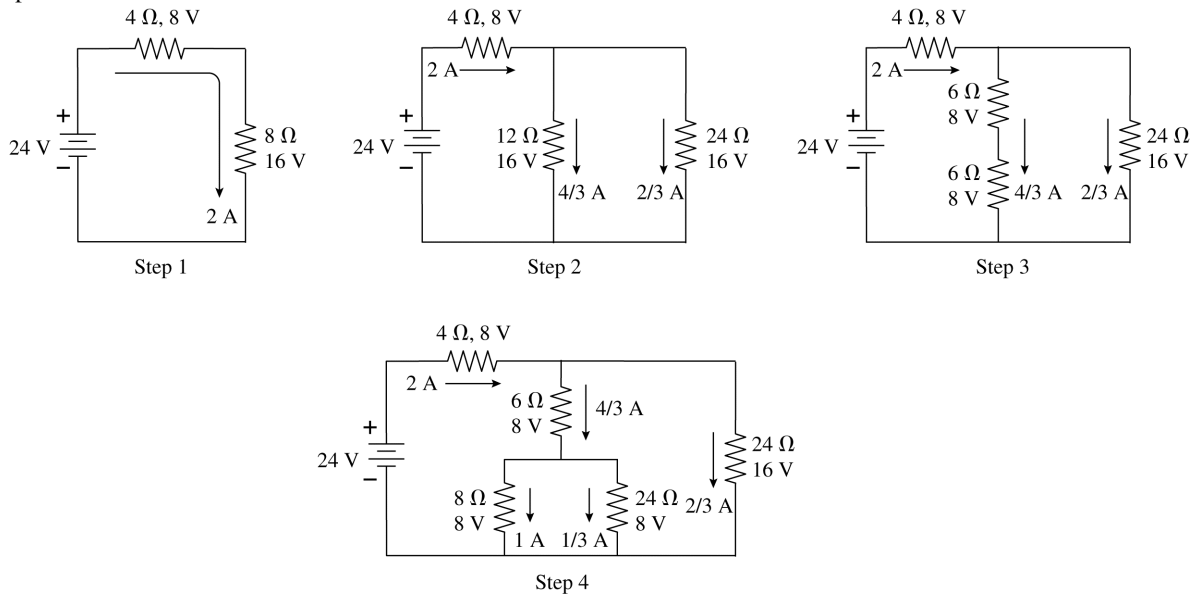
**31.69. Model:** The battery and the connecting wires are ideal.

**Visualize:**



The figure shows how to simplify the circuit in Figure P31.69 using the laws of series and parallel resistances. We will reverse the procedure and “build up” the circuit using the loop law and junction law to find the current and potential difference of each resistor.

**Solve:** Having found  $R_{eq} = 12\ \Omega$ , the current from the battery is  $I = (24\ \text{V})/(12\ \Omega) = 2.0\ \text{A}$ . As we rebuild the circuit, we note that series resistors *must* have the same current  $I$  and that parallel resistors *must* have the same potential difference  $\Delta V$ .



In Step 1 of the above figure, the  $12\ \Omega$  resistor is returned to  $4\ \Omega$  and  $8\ \Omega$  resistors in series. Both resistors must have the same  $2.0\ \text{A}$  as the  $12\ \Omega$  resistor. We use Ohm's law to find  $\Delta V_4 = 8\ \text{V}$  and  $\Delta V_8 = 16\ \text{V}$ . As a check,  $8\ \text{V} + 16\ \text{V} = 24\ \text{V}$ , which was  $\Delta V$  of the  $12\ \Omega$  resistor. In Step 2, the  $8\ \Omega$  resistor is returned to the  $12\ \Omega$  and  $24\ \Omega$  resistors in parallel. Both resistors must have the same  $\Delta V = 16\ \text{V}$  as the  $8\ \Omega$  resistor. From Ohm's law,  $I_{12} = (16\ \text{V})/(12\ \Omega) = \frac{4}{3}\ \text{A}$  and  $I_{24} = \frac{2}{3}\ \text{A}$ . As a check,  $I_{12} + I_{24} = 2.0\ \text{A}$ , which was the current  $I$  of the  $8\ \Omega$  resistor. In Step 3, the  $12\ \Omega$  resistor is returned to the two  $6\ \Omega$  resistors in series. Both resistors must have the same  $\frac{4}{3}\ \text{A}$  as the  $12\ \Omega$  resistor. We use Ohm's law to find  $\Delta V_6 = 8\ \text{V}$  and  $\Delta V_6 = 8\ \text{V}$ . As a check,  $8\ \text{V} + 8\ \text{V} = 16\ \text{V}$ , which was  $\Delta V$  of the  $12\ \Omega$  resistor. Finally, in Step 4, the  $6\ \Omega$  resistor is returned to the  $8\ \Omega$  and  $24\ \Omega$  resistors in parallel. Both resistors must have the same  $\Delta V = 8\ \text{V}$  as the  $6\ \Omega$  resistor. From Ohm's law,  $I_8 = (8\ \text{V})/(8\ \Omega) = 1\ \text{A}$  and  $I_{24} = \frac{1}{3}\ \text{A}$ . As a check,  $I_8 + I_{24} = \frac{4}{3}\ \text{A}$ , which was the current  $I$  of the  $6\ \Omega$  resistor.

Resistor	Potential difference (V)	Current (A)
$4\ \Omega$	8	2
$6\ \Omega$	8	$\frac{4}{3}$
$8\ \Omega$	8	1
Bottom $24\ \Omega$	8	$\frac{1}{3}$
Right $24\ \Omega$	16	$\frac{2}{3}$